

## Dynamical flow around a cylinder

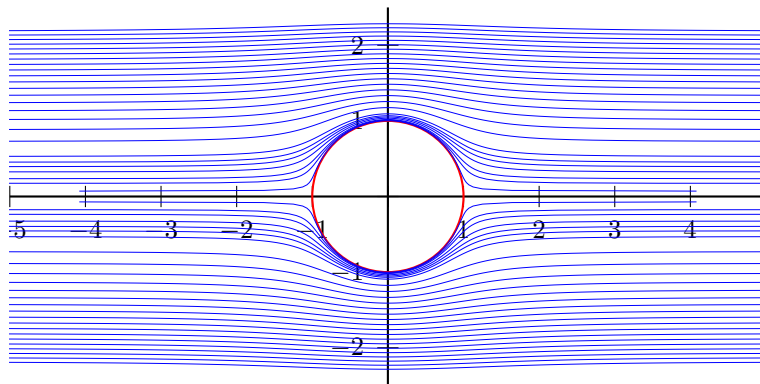
$$\left(r^2 - \frac{c_1}{r}\right) \sin^2 \theta = c_0$$

which is the same as

$$r^3 - \frac{c_0}{\sin^2 \theta} \cdot r - c_1 = 0$$

which can be solved by the formula of Cardano:

$$r^3 + 3pr + 2q = 0$$



Another possibility was shown by Manfred Braun<sup>1</sup> and gives a much more better result.

The potential flow around a cylinder has the complex potential

$$f(z) = u_\infty(z + a^2/z),$$

where  $u_\infty$  denotes the velocity at infinity and  $a$  is the radius of the cylinder.

The real and imaginary parts of  $f$  are the velocity potential  $\varphi$  and the stream function  $\psi$ , respectively. The streamlines are obtained by keeping  $\psi$  fixed and varying  $\varphi$ . They can be generated in the following way:

1. Solve the equation above for  $z = x + iy$  (simple quadratic equation).
2. Keep  $\psi = \Im f$  at a fixed value and use  $\varphi = \operatorname{Re} f$  as the parameter  $t$  in `parametricplot`. To this end the basic arithmetic operations for complex numbers, including the square root, have to be implemented.

The attached file generates a figure of the streamlines and equipotential lines around a cylinder. I have used my "personal" complex arithmetic PostScript command. (It would be more elegant to include them in a special style for complex calculations.)

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<sup>1</sup><http://www.tug.org/pipermail/pstricks/2004/001746.html>

